

## Cosmology Notes: Lecture 11

$$F_g = GMm/r^2$$

Where  $M$  and  $m$  are the masses of the two objects which have a mutual, attractive gravitational force,  $F_g$ . The two objects are separated by a distance  $r$ , measured from their centers. For spherical objects, gravity acts as if all the mass were concentrated at a point at their centers.

The concept of force,  $F$ , can be defined operationally as that which produces an acceleration according to Newton's second law:

$$F=ma$$

Colloquially, you can think of a force as a push or a pull

Note that the two masses,  $m$ , in the two equations have very different conceptual standing: In Newton's second law, the mass,  $m$ , represents a *sluggishness*, a resistance to being pushed or to having its momentum changed. It is *inertial* mass,  $m_i$ . In the gravitational law, though, the mass,  $m$ , is an interaction strength. It's completely analogous to charge,  $q$ , with respect to the electric force. This *gravitational* mass,  $m_g$ , dictates how strong the gravitational interaction will be with another massive object.

The equivalence of  $m_i$  and  $m_g$  is why all objects fall with the same acceleration due to gravity (on the surface of the Earth or of the Moon, say).

Comparing gravity on the surface of the Earth ( $r \sim 3200$  km, measured from the center of the Earth) to gravity in low-earth orbit (on the space shuttle, 300 km above the Earth's surface,  $r \sim 3500$  km), we find that it's only reduced by 16% in orbit. Why are astronauts "weightless"? ...They are in free-fall!

The astronaut floating in the space shuttle is like the sphere at the center of a first-law detector. ...Free-fall is a truly inertial reference frame!

Einstein's *equivalence principle* - the basis of general relativity:

***The effects of gravity and acceleration are indistinguishable.***

Stop thinking of gravity as a force.